

# Estimated Theoretical Models for Optical Constants for CuO<sub>2</sub> doped Polystyrene films

Mahasin F. Hadi Al-Kadhemy & Rana Ismael Khaleel

Al-Mustansiriya Univ.- College of Science- Physics Dept.

Baghdad/ IRAQ

Corresponding author: [drmahasinf@yahoo.com](mailto:drmahasinf@yahoo.com), [drmahasinf@gmail.com](mailto:drmahasinf@gmail.com)

## Abstract

An analysis study for optical constants of PS-CuO<sub>2</sub> thin films has been studied. The effect of doping percentage of CuO<sub>2</sub> to polystyrene films on the optical properties concluded from absorption and transmission measurements by using UV-VIS absorption spectrophotometer in the wavelength range (200-900nm). The refractive index (n), and extinction coefficient (k) have been evaluated experimentally and theoretically. Theoretical equation for refractive index (n) is:-

$$y = \frac{(a + cx)}{(1 + bx)}$$

And estimated theoretical equation for extinction coefficient (k) is:-

$$y = (a + cx^{0.5}) / (1 + bx^{0.5})$$

This was achieved by making fitting curves for all practical data using [Table curve 2D, version 5.01] program. This helps us to estimate a good similar data between experimental and theoretical results, and estimate any data that is not taken experimentally.

**Key words:** Optical Constants, Polystyrene Polymer, CuO<sub>2</sub>, Theoretical Model, Effect of Doping Percentage.

## 1- Introduction

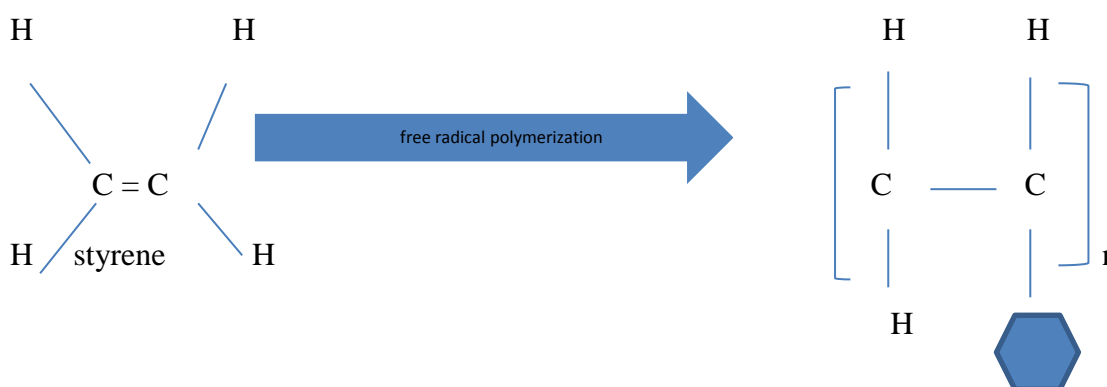
Plastic compounds are present in many target designs for inertial confinement fusion to achieve high gain. Moreover, experiments on fundamental processes such as hydrodynamic instabilities studies, have involved plastic as a basic material [1]. In recent years, polymers with different optical properties have been attracted much attentions due to their applications in the sensors [2], light-emitting diodes and others [3]. The optical properties of these materials can be easily tuned by controlling constants for different concentrations.

The addition of conductive fillers to the polymer giving a new product called as conducting polymer composite materials (CPCM) which consist of a random distribution of conducting throughout an insulating polymer [4]. The purpose of use of fillers can be divided

into two basic categories: - first, to improve the properties of materials and second, to reduce the cost of component [5].

The polymer used in this work is polystyrene. It is a perfect polymer for optical measurements [6], and immunological assays and soluble in aromatic hydrocarbon solvents, cyclohexane and chlorinated hydrocarbons.

Polystyrene is vinyl polymer[7],structurally, it is a long hydrocarbon chain, with a phenyl group attached to every other carbon atom is produced by free radical vinyl polymerization as shown in fig.(1)[8]:-



**Fig. (1) Chemical structure of polystyrene[8].**

Polystyrene, like other polymers, contains a very simple molecular structure [8], yet still exhibits many very interesting physical properties. For example, many scientists are still studying the radiation-induced reactions of polystyrene, as they show very complicated reactions despite their simple structures.

The optical behaviors of materials are utilized to determine their optical constants (refractive index (n), and extinction coefficient(k)).Several methods were proposed to determine the optical constants;they involve spectra photometric measurements of sample in the wavelength range[9].

The extinction coefficient (imaginary part of the refractive index) can be calculated by the relation[10]:-

$$K = \frac{\alpha \lambda}{4\pi} \quad (1)$$

Where ( $\lambda$ ) is the wavelength, ( $\alpha$ ) is the absorption coefficient which can be obtained using the following equation [11]:-

$$\alpha = \frac{2.3 \log \frac{1}{T}}{x} \quad (2)$$

Where(T) is the transmittance.

(x) is the thickness of the sample.

The refractive index (n) can be measured (when the reflectance (R) and (K) are Known) by using the equation [12]:-

$$n = \sqrt{\frac{4R(R+1)}{(R-1)^2 - K^2(R-1)}} \quad (3)$$

The optical study gives information about the fundamental properties of materials under investigation [13]. Analysis of the absorption spectra in the lower energy part gives information about atomic vibration while the higher energy part of the spectrum gives knowledge about the electronic states in the atom [14]. So that in the present work, we are studying the effect of additive on the optical properties of glassy polymer. The polymer used is polystyrene (PS) with additives ( $\text{CuO}_2$ ) in different concentrations. Also, we estimated theoretical models for this effect on two optical constants; the refractive index (n) and the extinction coefficient (K).

## 2- Experimental work

Polystyrene (PS), supplied by (ICI) company in the form of granules were used as matrix. Chloroform of purity 99.99 was used as a solvent. A dopant ( $\text{Cu}_2\text{O}$ ) was supplied by (Al-Sawari) company.

(PS) grains of weight (0.2) gm were dissolved in (5) ml of chloroform to obtain solution of 4% wt. /wt. The solution was shaken very well by hand for (1/2) hour or more to obtain homogenous mixture. Then, the mixture was cast into a glass sheet of dimensions ( $5 \times 5 \text{ cm}^2$ ) and kept in a dry atmosphere at ( $40^\circ\text{C}$ ) for (24) hours. The dried films were then removed easily using tweezers clamp.

The chosen concentrations of dopants relative to pure (PS) in (wt. /wt.) were (0.02, 0.04 and 0.06); the measurements of absorbance and transmittance spectra in the wavelength range (200-900nm) were carried out using UV/160/Shimadzu Spectrophotometer.

## 3- Results and Discussion

Our results involve experimental part and theoretical part as follow:-

### 3-1 Experimental part

The refractive index (n) of pure and doped PS with  $\text{CuO}_2$  were determined using eq.(3). Fig.(1) shows variation of (n) as a function of wavelength( $\lambda$ ), this figure showed that the (n) of doped PS increases with increasing ( $\lambda$ ) on the other hand (n) showed a systematic increase with increasing ( $\text{CuO}_2$ ) concentration [15].

The dependence of extinction coefficient ( $K$ ) on the wavelength obtained using eq.(1) is shown in Fig.(2) for pure and doped samples. It is noticed that ( $K$ ) value of pure sample has reduced becomes smaller at the region near the absorption edge, and becomes very small with increasing ( $\lambda$ ). While ( $K$ ) for doped sample with ( $\text{CuO}_2$ ) shows an increase with increasing ( $\lambda$ ). The maximum peaks belong to maximum absorption of ( $\text{CuO}_2$ ). Where ( $K$ ) shows an increase with increasing doping concentration (0.02, 0.04, 0.06) wt.%. The behavior of ( $K$ ) can be indicates that dopant atoms of ( $\text{CuO}_2$ ) will modify the structure of the host polymer [16].

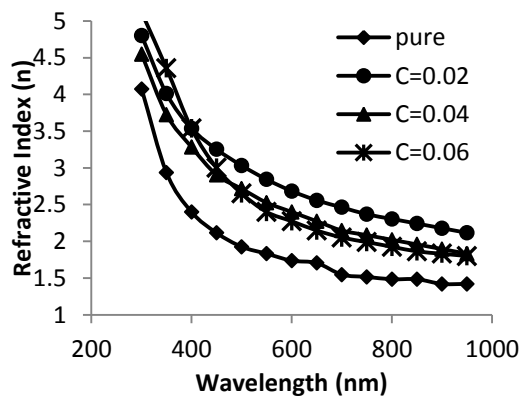


Fig.(2) Variation in refractive index ( $n$ ) as function of wavelength of pure and doped PS.

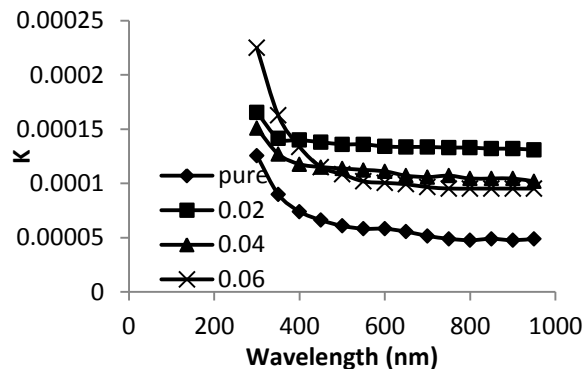
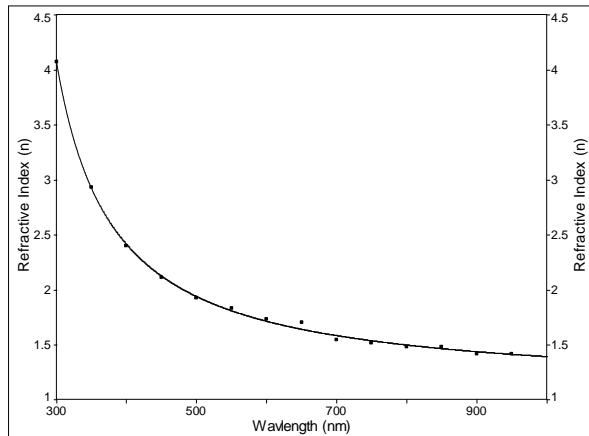


Fig.(3) Variation in extinction coefficient ( $K$ ) as function of wavelength of pure and doped PS.

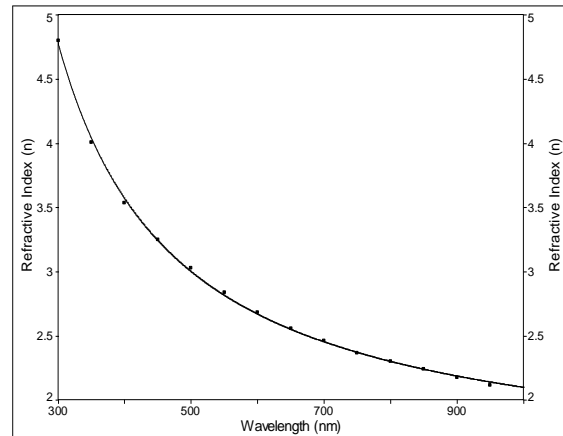
### 3-2 Theoretical Part

#### 3-2-1 Estimate Theoretical Model for Refractive Index

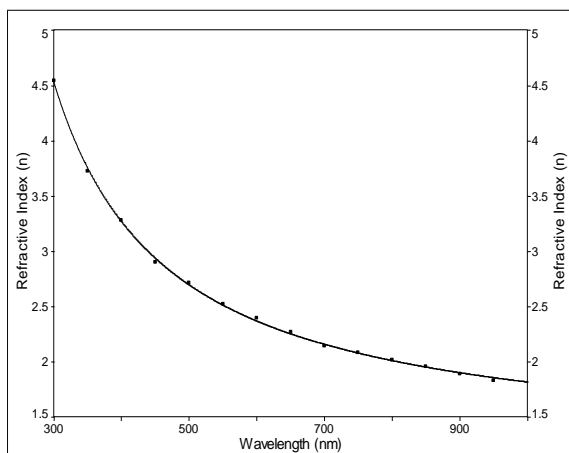
In Order to facility to estimate theoretical model for the effect of concentration of  $\text{CuO}_2$  doped PS and pure PS on the refractive index constant of optical properties, first we make a fitting curve to the relation between refractive index and wavelength for pure PS as shown in Fig.(4), and then we make a fitting curve to the relation between refractive index and wavelength for  $\text{CuO}_2$  (0.02) doped PS as shown in Fig.(5), and for  $\text{CuO}_2$  (0.04) doped PS as shown in Fig.(6), and for  $\text{CuO}_2$  (0.06) doped PS as shown in Fig.(7).



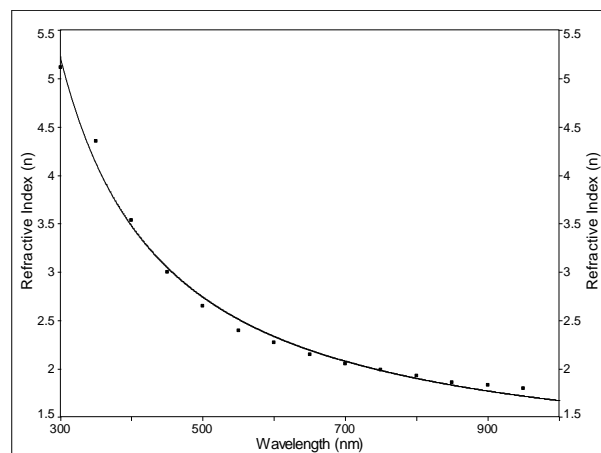
**Fig.(4) Fitting curve of the relation between refractive index and wavelength for pure PS**



**Fig.(5) Fitting curve of the relation between refractive index and wavelength for C=0.02 of CuO<sub>2</sub> doped PS**



**Fig.(6) Fitting curve of the relation between refractive index and wavelength for C=0.04 of CuO<sub>2</sub> doped PS**



**Fig.(7) Fitting curve of the relation between refractive index and wavelength for C=0.06 of CuO<sub>2</sub> doped PS**

The best estimated theoretical equation is:-

$$y = \frac{(a+cx)}{(1+bx)} \quad (4)$$

Where x and y act wavelength and refractive index, respectively. And  $a_1$ ,  $b_1$ , and  $c_1$  describe parameters of equation which varied with concentration of CuO<sub>2</sub>, and the value of these parameters illustrate in table (1).

Table (1)

The parameters of fitting equation for (n) constant for pure PS and different concentration of CuO<sub>2</sub>

Parameter	Pure PS	C=0.02	C=0.04	C=0.06
$r^2$	0.9988594599	0.9992872051	0.9993451737	0.9921811624
$a_1$	0.013619435	-3.45099035	-2.91623152	-3.10090992
$b_1$	-0.00452821	-0.00815927	-0.00739439	-0.00646628
$c_1$	-0.00493321	-0.01159357	-0.00872303	-0.00604506

Where  $r^2$  acts the correlation factor between experimental and theoretical data.

The  $a_1$ ,  $b_1$  and  $c_1$  parameters plotted against concentration of CuO<sub>2</sub> as shown in figs. (8-10), respectively. The fitting equations of these figures are written above each figure.

$$y_1 = \frac{(0.011214469 - 798089.84x_1^2)}{(1 + 251864.3x_1^2)} y_2$$

$$= 0.17338662 - 0.049892527x_1^{0.5}$$

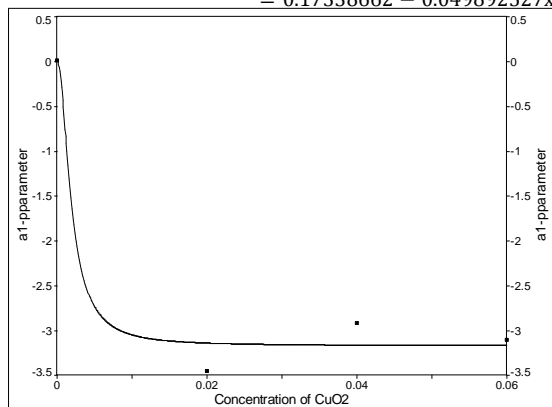


Fig.(8) The relation between concentration of CuO<sub>2</sub> and  $a_1$ -parameter.

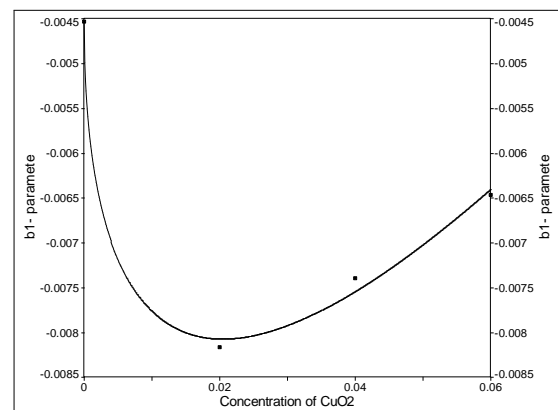
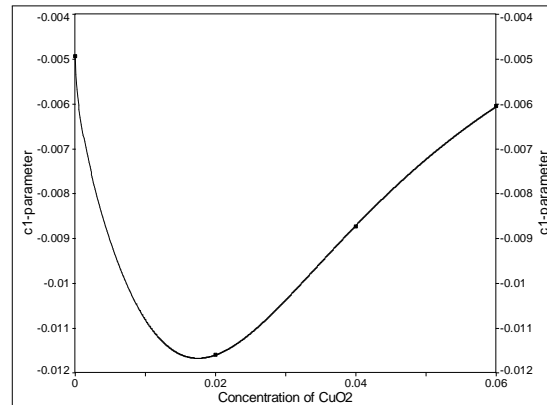


Fig.(9) The relation between concentration of CuO<sub>2</sub> and  $b_1$ -parameter.

$$y_3 = -7062.9181 + 1785.0308x_1^{0.5} + 6860.0933e^{(-x_1)}$$



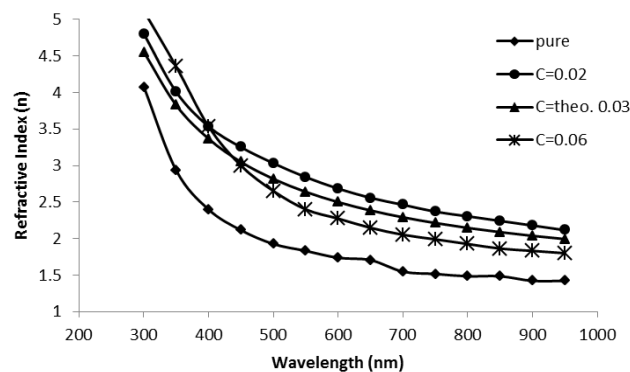
**Fig.(10) The relation between concentration of  $\text{CuO}_2$  and  $c_1$ -parameter.**

Where  $y_1, y_2$  and  $y_3$  in fitting equations represent  $a_1, b_1$  and  $c_1$  parameters, respectively, and  $x_1$  represent the concentration of  $\text{CuO}_2$ . We choose test concentration  $\text{CuO}_2$  as  $C=0.03$  to prove our model.

The estimated theoretical equation for test concentration of  $\text{CuO}_2$   $C=0.03$  is:-

$$y = \frac{(-3.1547623 - 0.010374005x)}{(1 - 0.0079216x)} \quad (5)$$

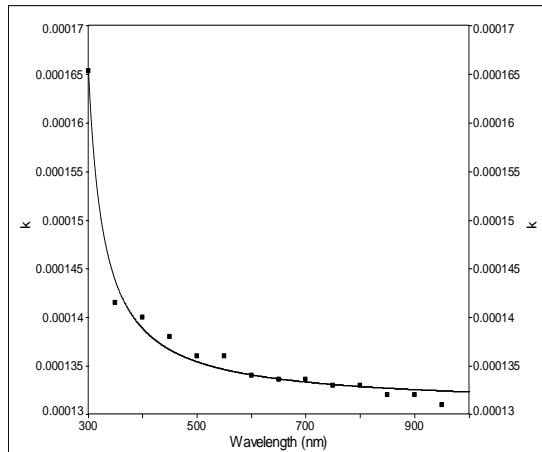
Then plotted this test concentration with experimental curves, as in fig.(11).this is a good matching between the behavior of these curves(experimental and theoretical).



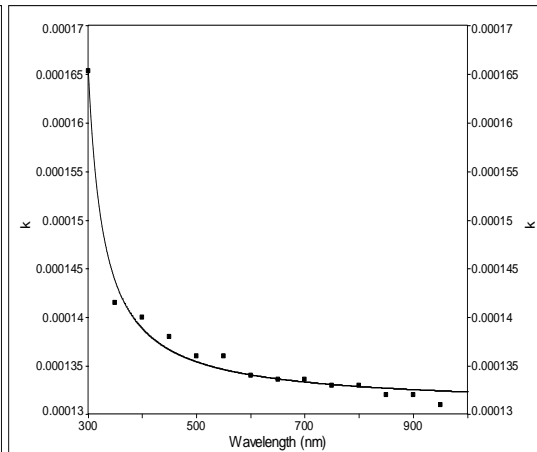
**Fig.(11) Theoretical and experimental relation between refractive index and wavelength for pure PS and different concentration of  $\text{CuO}_2$  doped PS.**

### 3-2-2 Estimate Theoretical Model for Extinction Coefficient

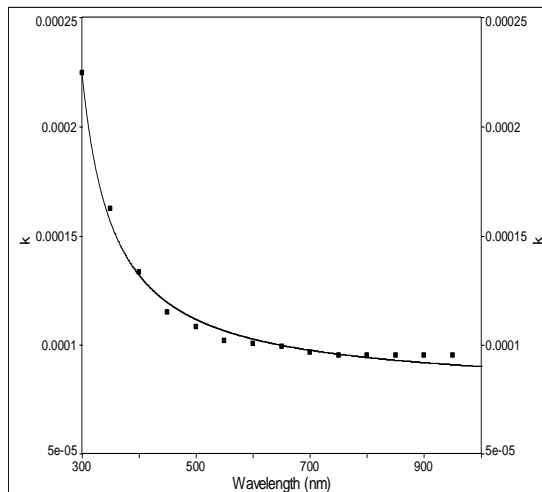
In Order to facility to estimate theoretical model for the effect of concentration of  $\text{CuO}_2$  doped PS and Pure PS on the extinction coefficient (K) constant of optical properties; fig. (3). First we make a fitting curve to the relation between extinction coefficient and wavelength for pure PS as shown in Fig(12),and then we make a fitting curve to the relation between extinction coefficient and wavelength for  $\text{CuO}_2$  (0.02) doped PS as shown in Fig.(13),and for  $\text{CuO}_2$ (0.04) doped PS as shown in Fig(14),and for  $\text{CuO}_2$ (0.06)doped PS as shown in Fig(15).



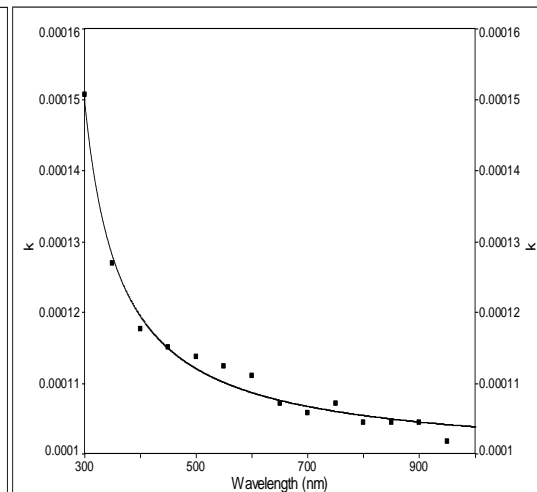
**Fig.(12) Fitting curve of the relation Between extinction coefficient and wavelength for pure PS.**



**Fig.(13)Fitting curve of the relation betweenrefractive index and wavelength for C=0.02 of  $\text{CuO}_2$  doped PS**



**Fig. (14) Fitting curve of the relation between extinction coefficient and wavelength for C=0.04 of  $\text{CuO}_2$  doped PS.**



**Fig. (15) Fitting curve of the relation between extinction coefficient and wavelength for C=0.06 of  $\text{CuO}_2$  doped PS.**



The estimated theoretical equation is:-

$$y_4 = (a_2 + c_2 x^{0.5}) / (1 + b_2 x^{0.5}) \quad (6)$$

Where  $y_4$  represent extinction coefficient  $K$  and  $x$  act wavelength  $\lambda$ . The value of  $a_2$ ,  $b_2$ , and  $c_2$  parameters illustrate in table (2).

Table (2)

The parameters of fitting equation for pure PS for different concentration of  $\text{CuO}_2$

Parameter	Pure PS	C=0.02	C=0.04	C=0.06
$r^2$	0.99624357	0.98681115	0.98705963	0.99237414
$a_2$	2.3183429e-6	0.00012858181	9.1272919 e-5	5.8869836 e-5
$b_2$	-0.065546553	-0.060722186	-0.06479445	-0.063755775
$c_2$	-2.3205228 e-6	-7.9170928 e-6	-6.3315171 e-6	-4.7601023 e-6

Where  $r^2$  act the correlation factor between experimental and theoretical data, The fitting equation of these figures are written above each figure.

$$y_4 = 4 * 0.000127442 n(1 - n) y_5 = -0.06635617 - \frac{0.05208961}{\ln x} - 0.13279786 / (\ln x_1)^2$$

Where  $n = \exp\left(-\frac{x_1 + 0.00145884}{0.029603538}\right)$

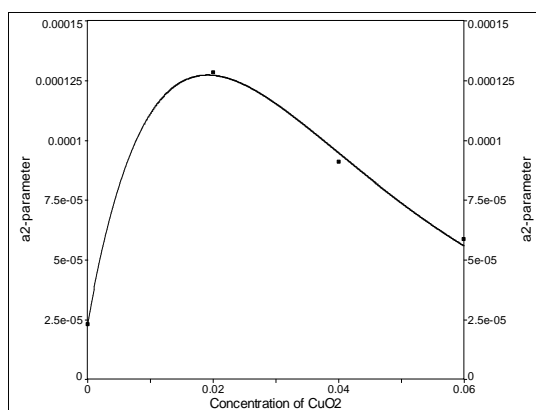


Fig. (16) The relation between concentration of  $\text{CuO}_2$  and a-parameter

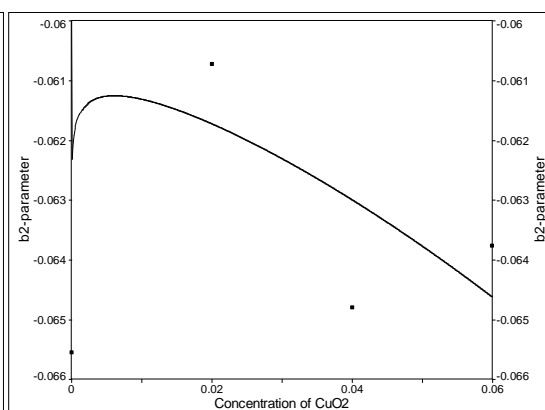
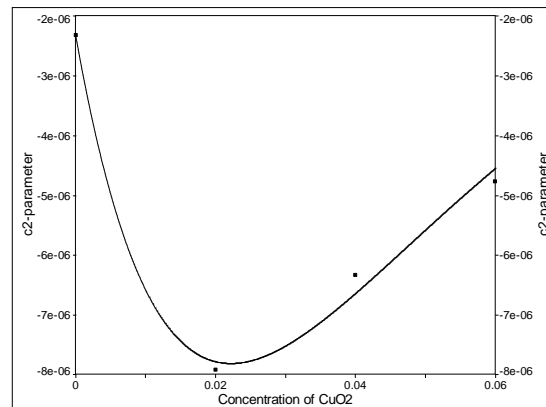


Fig. (17) The relation between concentration of  $\text{CuO}_2$  and b-parameter

$$y_6 = -4 * 7.8119e - 6 n(1 - n)$$

Where  $n = \exp(-x_1 + 0.00308849) / 0.036358276$



**Fig. (18) The relation between concentration of CuO<sub>2</sub> and c-parameter**

Two test concentrations of CuO<sub>2</sub>, C=0.05 and C=0.08 where chosen to estimate the theoretical model.

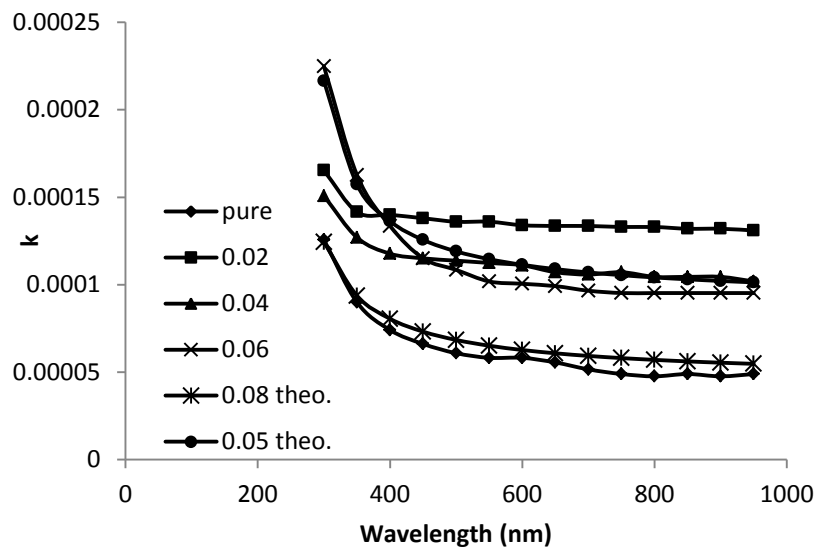
The estimated theoretical equation for C=0.05 is:-

$$y_4 = (7.387e^{-5} - 2.8558e^{-6}x)^{0.5} / (1 - 0.06655x)^{0.5} \quad (7)$$

And the estimated theoretical equation for C=0.08 is:-

$$y_4 = (3.046e^{-5} - 2.8558e^{-6}x)^{0.5} / (1 - 0.06655x)^{0.5} \quad (8)$$

Then experimental and theoretical curves were plotted in fig.(19). All these curves have the same type in behavior, so that we can plot any data for K coefficient for this material without make it experimentally. This is matched with results obtained by Al-kadhemy[17], Al-Kadhemy et al [18].



**Fig. (19) Theoretical and experimental relation between extinction coefficient and wavelength for pure PS and different concentration of CuO<sub>2</sub> doped PS.**

## 4- Conclusion

The ability of estimating theoretical models from practical data for the effect of doping percentage of CuO<sub>2</sub> to polystyrene films on the optical properties ; refractive index (n) and extinction coefficient (K) was deduced in this work. Very well theoretical results and matched with the behavior of practical results.

## 5- References

- [1] Omar M.A.,(1993),Elementary Solid State Physics,Addison-Wesley Publishing Company.
- [2] Grazulevicius J.V., Strohmriegl P., Pielichowski J.,(2003), Carbazole-Containing Polymers: Synthesis, Properties and Applications, Prog. Polym. Sci., 28(9):PP:1297-1353.
- [3] Mansour S.F.,(2000), Frequency and Composition dependence on the Dielectric Properties for Mg-Zn Ferrit, Egypt. J. Solids,V.(28),No.(2) ,PP.263.
- [4] Gubbels F., Blacler. S., Vanlathem E. ,Jerome R., Veltoure R.,and Brouse F.,(1995), PhD. Teyssie, Conductive Polymer Composite Materials and methods of making Same,Macromolecules,28,PP:1559-1566.
- [5] Rainer H.,(2008), Technical Notes and Applications for Laboratory Work, 3, PP: 1-7.

- [6] Nicholas P., (1997), Handbook of Engineering Polymeric Materials, Marcel Dekker, New York, PP:137-138.
- [7] Zbigniew D. Jastrzebski,(1977),The Nature and Properties of Engineering Materials,John Wiley and Sons,New York,PP:373-418.
- [8] Al-Kadhemy M. F. Hadi, S.Sanaa R., H. Haider S., H. Wafaa A.,(2013), Effect of Gamma Radiation on Optical Energy Gap of Crystal Violet Doped Polystyrene Films, IJAIEM ,Volume 2, Issue 5, pp. 511-516.
- [9] Pankov J.,(1971), Optical Processes in Semiconductors,London.
- [10] Molt N. and Davis E.,(1971), Electronic Process in Non-Crystalline Materials,2<sup>nd</sup> edition,University Press,Oxford.
- [11] Saferaza M., Heppenstall Butter M., Gubitt R., Bucknall D., Webster J., Jones R.A.L.,(1998), Phys.Rev.Lett.,81,PP:5173.
- [12] Jenkins. F. A., and White. H.E., (2010), Fundamentals of Optics,4<sup>th</sup> edition.
- [13] Padhyay. B., Bhijit A., Basak C.,(2007), Studies on Photo catalytic degradation of Polystyrene, Materials Science and Technology,23(3),PP:307-317.
- [14] Hameed Al-Attar, (2003), A new highly photorefractive polymer composite for Optical data storage application,Pure Appl. Opt.,5, PP. S487-S492.
- [15] Ahmed A.H.,Awaitf A.M. and Zaeid Abdul-Majied N.,(2007),Dopping Effect on Optical Constants of (PMMA),Eng. & Technology,Vol.25,No.4.
- [16] Srivastava S., Haridas M., and Basu. J. K.,(2008), Optical Properties of Polymer Nanocomposites, Bull. Mater. Sci., Vol. (31), PP: 213-217.
- [17] Al-Kadhemy M.F. Hadi, (2012), Effect of thickness of CdTe/Ge heterojunction photo detectors on optoelectronic properties, Physica B, 407(17), pp. 3335-3338.
- [18] Al-Kadhemy M.F. Hadi, Husain R., Al-Zuky A. A. Dawood, (2012),Analysis of the Absorption Spectra of Styrene-butadiene in Toluene, j. of Physical Science, Vol. 23(1), pp. 89–100.

This academic article was published by The International Institute for Science, Technology and Education (IISTE). The IISTE is a pioneer in the Open Access Publishing service based in the U.S. and Europe. The aim of the institute is Accelerating Global Knowledge Sharing.

More information about the publisher can be found in the IISTE's homepage:

<http://www.iiste.org>

## CALL FOR JOURNAL PAPERS

The IISTE is currently hosting more than 30 peer-reviewed academic journals and collaborating with academic institutions around the world. There's no deadline for submission. **Prospective authors of IISTE journals can find the submission instruction on the following page:** <http://www.iiste.org/journals/> The IISTE editorial team promises to the review and publish all the qualified submissions in a **fast** manner. All the journals articles are available online to the readers all over the world without financial, legal, or technical barriers other than those inseparable from gaining access to the internet itself. Printed version of the journals is also available upon request of readers and authors.

## MORE RESOURCES

Book publication information: <http://www.iiste.org/book/>

Recent conferences: <http://www.iiste.org/conference/>

## IISTE Knowledge Sharing Partners

EBSCO, Index Copernicus, Ulrich's Periodicals Directory, JournalTOCS, PKP Open Archives Harvester, Bielefeld Academic Search Engine, Elektronische Zeitschriftenbibliothek EZB, Open J-Gate, OCLC WorldCat, Universe Digital Library, NewJour, Google Scholar

